

## **Department of Mathematics**

Name of Teacher	: Dr. Nirmal Singh		
Designation	: Assistant Professor		
	<b>B.Sc. (Mathematics) Third Year</b>		
	<b>Course Code</b>	: MATH304TH	
	Name of the Course	: Numerical Methods	

**Course Learning Outcomes**: On successful completion of this course, the student will be able to

**CO1.** Understand numerical techniques to find the roots of non-linear equations and solution of system of linear equations.

**CO2.** Understand the difference operators and the use of interpolation.

**CO3.** Understand numerical differentiation and integration and numerical solutions of ordinary and partial differential equations.

**CO4.** Demonstrate understanding of common numerical methods and how they are used to obtain approximate solutions to otherwise intractable mathematical problems.

**CO5.** Apply numerical methods to obtain approximate solutions to mathematical problems

**CO6.** Derive numerical methods for various mathematical operations and tasks, such as interpolation, differentiation, integration, the solution of linear and nonlinear equations, and the solution of differential equations

CO7. Analyse and evaluate the accuracy of common numerical methods

#### Plan of Teaching the Subject According to Syllabus

Lecture 1 Introduction to Syllabus and some basic concepts required for it

- Lecture 2 Introduction to Algorithm
- Lecture 3 Order of Convergence of various methods
- Lecture 4 Bisection method for solving polynomial equations
- Lecture 5-7 Examples based on Bisection method
- Lecture 8 Explanation of working of False position method
- Lecture 9-11 Examples based on False position method
- Lecture 12 Explanation of working of Fixed point iteration method
- Lecture 13-14 Examples based on Fixed point iteration method
- Lecture 15 Explanation of working of Newton's method
- Lecture 16-17 Examples based on Newton's method
- Lecture 18 Explanation of working of Secant method
- Lecture 19 Examples based on Secant method
- Lecture 20 Explanation of working of LU decomposition
- Lecture 21-22 Examples based on LU decomposition
- Lecture 23 Class test of Unit 1
- Lecture 24 Explanation of working of Gauss-Jacobi
- Lecture 25 Examples based on Gauss-Jacobi
- Lecture 26 Explanation of working of Gauss-Siedel
- Lecture 27 Examples based on Gauss-Siedel
- Lecture 28 Explanation of working of SOR iterative methods
- Lecture 29 Examples based on SOR iterative methods
- **Lecture 30** Explanation of working of Newton Forward and backward interpolation formulas
- Lecture 31-32 Examples based on Newton Forward and backward interpolation formulas
- Lecture 33 Explanation of working of Newton divided interpolation formula
- Lecture 34-35 Examples based on Newton divided interpolation formula
- Lecture 36 Explanation of working of Lagrange interpolation formula
- Lecture 37-38 Examples based on Lagrange interpolation formula
- Lecture 39 Class test of Unit 2

Lecture 40 Explanation of working of Finite difference operators

**Lecture 41** Explanation of working of Numerical differentiation: Newton's forward difference and backward difference method

Lecture 42-44 Examples based on Numerical differentiation: Newton's forward difference and backward difference method

Lecture 45 Explanation of working of Sterling's Central difference method

Lecture 46-48 Examples based on Sterling's Central difference method.

Lecture 49 Class test of Unit 3

Lecture 50 Explanation of working of Trapezoidal rule

Lecture 51 Examples based on Trapezoidal rule

Lecture 52 Explanation of working of Simpson's rule 1/3 and 3/8

Lecture 53-54 Examples based on Simpson's rule 1/3 and 3/8

Lecture 55 Explanation of working of Euler's method and modified Euler's method

Lecture 56-58 Examples based on Sterling's Euler's method and modified Euler's method

Lecture 59 Class test of Unit 4

Lecture 60 Discussion about Annual Exams & preparation techniques.

# B.Sc. (Mathematics) Third Year Course Code : MATH317TH Name of the Course : Transportation And Game Theory

#### **Course Learning Outcomes:**

After the successful completion of this course, it is indented that a student will be able to: **CO1.** To develop formulation skills in transportation models and finding solutions **CO2.** To understand the basics in the field of game theory and assignment problems

**CO3.** Interpret the transportation models' solutions and infer solutions to the real-world problems

CO4. Recognize and solve game theory and assignment problems.

CO5. Knowledge of drawing project networks for quantitative analysis of projects

**CO6.** Know when simulation and dynamic programming can be applied in real world problems

## Plan of Teaching the Subject According to Syllabus

Lecture 1 Introduction to Transportation problem Lecture 2 Mathematical formulation of Transportation problem with Examples Lecture 3 Mathematical formulation of Transportation problem with Examples Lecture 4 Mathematical formulation of Transportation problem with Examples Lecture 5 Northwest-corner method mathematical working Lecture 6 Northwest-corner method mathematical working explanation with examples Lecture 7-8 Northwest-corner method mathematical working explanation with examples Lecture 9 Least cost method mathematical working explanation with examples Lecture 10 Least cost method mathematical working explanation with examples Lecture 11-12 Least cost method mathematical working explanation with examples Lecture 13-14 Discussion about various problems in Unit 1.

Lecture 15 Class test of Unit 1.

Lecture 16 Vogel approximation method for determination of starting basic solution explanation

Lecture 17-19 Examples of Vogel approximation method for determination of starting basic solution

Lecture 20 Explanation of algorithm for solving transportation problem

Lecture 21-24 Examples on algorithm for solving transportation problem

Lecture 25 Class test of Unit 2

Lecture 26 Explanation of Assignment problem and its mathematical formulation

Lecture 27-28 Examples on Assignment problem and its mathematical formulation

Lecture 29 Explanation of Hungarian method for solving assignment problem

Lecture 30-34 Examples on Hungarian method for solving assignment problem

Lecture 35 Class test on Unit 3

Lecture 36 Explanation of formulation of two person zero sum games

Lecture 37-40 Explanation and Example on solving two person zero sum games

Lecture 41-43 Explanation and Example on games with mixed strategies

Lecture 44-45 Explanation and Example on graphical solution procedure for games

Lecture 46 Class test of Unit 4

Lecture 47 Discussion about Annual Exams & preparation techniques.

#### M.Sc. (Mathematics) First Semester

# Course Code: M-102Name of the Course: Advanced Algebra I

Course Learning Outcomes: On completion of the course, students shall be able to

CO1 Develop the understanding about the importance of group actions on sets.

**CO2** Describe the normal series, solvable groups, nilpotent groups and their applications to characterize some classes of groups.

CO3 Have the broad idea about direct sum and direct product of groups.

**CO4** Have the knowledge about finitely generated Abelian groups which are decomposable as a finite direct sum of cyclic groups which enables the students to find the number of non-isomorphic Abelian groups of given order.

**CO5** Understand the Sylow Theorems and their applications: in particular, the existence of a simple group of a given order.

**CO6** Provide the comprehensive understanding of ring theory and some special classes of rings such as Quotient rings, Euclidean rings, ring of Gaussian integers and Polynomial rings over the Rational fields and Commutative rings.

**CO7** Have knowledge of the concept of Modules, free modules, completely reducible modules and Quotient modules.

## Plan of Teaching the Subject According to Syllabus

Lecture 1 Introduction to Syllabus and benefits of learning it

Lecture 2 Conjugacy and G-Sets

Lecture 3 Normal Series

- Lecture 4 Solvable Groups
- Lecture 5 Nilpotent Groups

Lecture 6 Direct Products

#### Lecture 7-8 Finitely Generated Abelian Groups

Lecture 9 Least cost method mathematical working

Lecture 10 Invariants of a Finite abelian Groups

Lecture 11-12 Sylow Theorems

Lecture 16 Definition and Examples of Rings Lecture 17-19 Some Special Classes of Rings Lecture 20 Homomorphisms Lecture 21-24 Ideals and Quotient Rings Lecture 21-24 More Ideals and Quotient Rings and The Field of Quotients of an Integral Domain. Lecture 25 Euclidean Rings, a Particular Euclidean Ring Lecture 26, Polynomial Rings Lecture 27-28 Polynomials over the Rational Field Lecture 29 Polynomial Rings over Commutative Rings Lecture 35 Class test on Unit 3 Lecture 36 Definition and examples, Submodules and direct sums Lecture 37-40, homomorphisms and quotient modules Lecture 41-43 Completely reducible modules Lecture 44-45 Free modules Lecture 46 Class test of Unit 3

Lecture 47 Discussion about Annual Exams & preparation techniques.

Lecture 13-14 Groups of Orders p2, pq

Lecture 15 Class test of Unit 1.

# M.Sc. (Mathematics) Second Semester Course Code : M-202 Name of the Course : Field Theory

Course Learning Outcomes: On completion of the course, students shall be able to

**CO1** Develop the understanding about the reducible and irreducible polynomials and their roots.

CO2 Identify the relations of one field to another (known as the concept of field extension).

**CO3** Have the knowledge of field extensions, Algebraic extensions, Normal extensions, algebraically closed fields and Splitting fields.

**CO4** Have a broad idea of some special types of fields such as Prime fields, finite fields, roots of unity and cyclotomic polynomials. In particular, the representation of elements of finite fields.

**CO5** Understand the Galois Theory which creates a bridge to move from a field to a group, and make some remarkable observations using group theory.

**CO6** Have a knowledge of separable extensions, automorphism group and fixed fields fundamental theorems of Galois theory and algebra.

## Plan of Teaching the Subject According to Syllabus

- Lecture 1 Introduction to Syllabus and benefits of learning it
- Lecture 2 Irreducible polynomials and Eisenstein criterion

Lecture 3 Adjunction of roots

Lecture 4 Algebraic extensions

Lecture 5 Algebraically closed fields

Lecture 6 Splitting fields

- Lecture 7-8 Normal extensions
- Lecture 9-10 Multiple roots
- Lecture 12 Class test of Unit 1.

Lecture 13 Prime Fields

- Lecture 14-16 Finite fields
- Lecture 17 Roots of Irreducible Polynomials

Lecture 18-19 Roots of unity and cyclotomic polynomials

Lecture 20-22 Representation of Elements of Finite Fields

Lecture 23-24 Order of Polynomials and Primitive Polynomials

Lecture 25 Irreducible Polynomials

Lecture 26 Class test on Unit 2

Lecture 27 Separable extensions

Lecture 28-29 Automorphism groups and fixed fields

Lecture 30-33 Fundamental theorem of Galois theory

Lecture 34-35 Fundamental theorem of algebra

Lecture 36 Class test of Unit 3

Lecture 37 Discussion about Annual Exams & preparation techniques.

M.Sc. (Mathematics) Third Semeste		
Course Code	: M-303	
Name of the Course	: Topology	

Course Learning Outcomes: On completion of the course, students shall be able to

CO1 Develop the understanding about the partial ordered relations and lattices.

**CO2** Understand some elementary concepts in metric spaces and topological spaces such as open bases, open subbases, weak topology and the function algebras.

**CO3** Identify the open sets, closed sets, convergence and continuity in metric/topological spaces.

**CO4** Have a broad idea of compactness and various separation axioms in a topological space using some remarkable theorems such as Tychonoff's theorem, the Urysohn imbedding theorem, Ascoli's theorem, Urysohn's lemma and Tietze's theorem.

**CO5** Understand connectedness in topological spaces, connected components, locally connected spaces and totally disconnected spaces.

**CO6** Have a knowledge of The Weierstrass approximation theorem used to approximate a real valued continuous function by a real polynomial

#### Plan of Teaching the Subject According to Syllabus

Lecture 1 Introduction to Syllabus and benefits of learning it

Lecture 2 Partial ordered sets and lattices.

Lecture 3 Open sets

Lecture 4 closed sets

Lecture 5 Algebraically closed fields

Lecture 6 Convergence

Lecture 7 Completeness

Lecture 8 Baire's category theorem

Lecture 9 Continuity

Lecture 10 The definition and some examples

Lecture 11 Completeness

Lecture 12 Elementary concepts, Open bases and open subbases

- Lecture 13 Weak topologies
- Lecture 14 the function algebras C (X, R) and C (X, C)
- Lecture 15 Class test of Unit 1.
- Lecture 16 Compact spaces
- Lecture 17 Products of spaces
- Lecture 18 Tychonoff's theorem and locally compact spaces
- Lecture 19 Compactness for metric spaces
- Lecture 20 Ascoli's theorem
- Lecture 21 T1-spaces and Hausdorff spaces
- Lecture 22 Completely regular spaces and normal spaces
- Lecture 23 Urysohn's lemma and Tietze's extension theorem
- Lecture 24 The Urysohn imbedding theorem
- Lecture 25 The Stone-Cech compactification.
- Lecture 26 Class test on Unit 2
- Lecture 27 Connected spaces
- Lecture 28 The components of a space
- Lecture 29 Totally disconnected spaces
- Lecture 30 Locally connected spaces.
- Lecture 31 The Weierstrass approximation theorem
- Lecture 32 Class test of Unit 3
- Lecture 33 Discussion about Annual Exams & preparation techniques.

# M.Sc. (Mathematics) Fourth Semester Course Code : M-401 Name of the Course : Functional Analysis

Course Learning Outcomes: On completion of the course, students shall be able to

CO1 Develop the understanding about the Normed linear spaces and Banach spaces.

**CO2** Have the knowledge of continuous linear transformations between normed linear spaces and the concept of dual spaces, double dual and reflexive spaces.

**CO3** Have a broad idea of some important results such as The Hahn-Banach theorem, the open mapping theorem, the closed graph theorem and the Uniform Boundedness theorem.

**CO4** Understand Hilbert spaces, its conjugate space, adjoint of an operator, self-adjoint, normal and unitary operators and projections.

**CO5** Describe the spectral theory in normed spaces, spectral properties of Bounded linear operators, Banach algebra and its properties.

CO6 Apply the knowledge of Complex Analysis in Spectral theory

#### Plan of Teaching the Subject According to Syllabus

- Lecture 1 Introduction to Syllabus and benefits of learning it
- Lecture 2 The definition and some examples
- Lecture 3 Continuous linear transformations
- Lecture 4-5 The Hahn- Banach Theorem
- Lecture 6-7 The Open Mapping Theorem
- Lecture 8 The Closed Graph Theorem
- Lecture 9-10 Uniform Boundedness Theorem
- Lecture 11-12 The natural embedding of N in N\*\*

Lecture 13 Reflexivity

Lecture 14 Class test of Unit 1

Lecture 15 The definition and some simple properties

- Lecture 16 Orthogonal complements
- Lecture 17 Orthonormal sets
- Lecture 18 Conjugate space H\*
- Lecture 19 The adjoint of an operator
- Lecture 20-21 Self-adjoint normal and unitary operators
- Lecture 22-23 Projections
- Lecture 24 Class test on Unit 2
- Lecture 25 Spectral Theory in Finite Dimensional Normed Spaces
- Lecture 26 Spectral Properties of Bounded Linear Operators
- Lecture 27-28 Further Properties of Resolvent and Spectrum
- Lecture 29-30 Use of Complex Analysis in Spectral Theory.
- Lecture 31 Further Properties of Banach Algebras
- Lecture 32 Class test of Unit 3
- Lecture 33 Discussion about Annual Exams & preparation techniques.